# Swing Set Sinusoids and variations 

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## HS Math on the Playground

- See Saw variation-for Algebra 2 mass vs. distance
- Swing Problem—for Precalculus trigonometric models



## Math on a See Saw Introduction by the younger generation

- Watch the video and think about the variables are involved in what you see changing
- How are the variables related?
- Ideas for classroom simulation with data collection?

From: http://www.peepandthebigwideworld.com/en/kids/videos/87/seesaw-science/

## In situations involving motion ...

- Take time to think about what is varying
- How many quantities vary here?



## Time to Swing



## Swing Problem

- Watch the video and think about breaking up the swinger's position into her vertical and horizontal positions.
- We will use parametric equations and our knowledge of graphs of trigonometric functions to model her position over time
- Video by Marian Hernandez from NCSSM


## Video time



## Questions to consider:

- What types of functions should we use to model her motion?
- Quadratic?
- Sinusoidal?
- How are the periods of her horizontal motion and vertical motion related?
- What assumptions are we making with our model?
- What would happen if we "start" our time values when she is in the "middle" of her swing?


## Using Logger Pro

- Free trial for 1 month, maybe free download?
- Switch to Logger Pro. https://www.vernier.com/product/logger-pro-3/
- Insert movie
- Set origin
- Set scale
- Collect data


## Collecting data

No Device Connected

|  | VideoAnalysis |  |
| :---: | :---: | :---: | :---: |
|  | Y <br> $(\mathrm{m})$ | Vx <br> $(\mathrm{m} / \mathrm{s})$ |
| 1 | -1.581 | 6.662 |
| 2 | -2.434 | 6.692 |
| 3 | -2.431 | 5.867 |
| 4 | -2.413 | 6.505 |
| 5 | -2.365 | 9.005 |
| 6 | -2.287 | 8.800 |
| 7 | -2.163 | 7.761 |
| 8 | -2.041 | 5.087 |
| 9 | -2.034 | 4.196 |
| 10 | -1.872 | 4.504 |
| 11 | -1.872 | 6.308 |
| 12 | -1.523 | 6.438 |
| 13 | -1.317 | 3.040 |
| 14 | -1.317 | 2.560 |
| 15 | -1.116 | 3.304 |
| 16 | -0.9591 | 3.267 |
| 17 | -0.7797 | 2.475 |
| 18 | -0.6211 | 1.315 |
| 19 | $-0.642 €$ | 0.772 |
| 20 | -0.4807 | 0.800 |
| 21 | -0.3487 | 0.661 |
| 22 | -0.2862 | 0.552 |
| 23 | -0.2017 | 0.377 |
| 24 | $-0.178 €$ | 0.347 |
| 25 | $-0.124 \Xi$ | 0.335 |
| 26 | -0.0924 | 0.153 |
| 27 | $-0.097 \varepsilon$ | -0.018 |
| 28 | $-0.097 \varepsilon$ | -0.259 |
| 29 | $-0.097 \varepsilon$ | -0.899 |
| 30 | -0.2125 | -1.158 |
| 31 | $-0.345 \equiv$ | -0.811 |
| 32 | $-0.447 \Xi$ | -0.498 |
| 33 | $-0.503 \ell$ | -0.136 |
| 34 | -0.4485 | -0.515 |
|  |  |  |
|  |  |  |



## Desmos images

- Graphs



## Let's experiment

- Get a handout
- Get tools—heavy lock or washer, string, meter (or yard) stick
- Time-keeping device (watch, phone, stopwatch)
- Design experiment

Student handout:
https://drive.google.com/file/d/1UtgRiMOUr08Oittt6wnGzlOo2ovLzrk6/view?usp=sharing


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